

Name _____

Determine if the function is one-to-one. Explain your answer.

1) $f(x) = 7x + 7$

2) $f(x) = 5x + 5$

3) $f(x) = x^3 - 4$

4) $f(x) = x^3 - 7$

5) $f(x) = x^2 - 2$

6) $f(x) = x^2 + 6$

7) $f(x) = -(x - 6)^2$

8) $f(x) = -(x - 10)^2$

9) $f(x) = |x + 3|$

10) $f(x) = |x + 4|$

11) $h(x) = \frac{x - 8}{5}$

12) $h(x) = \frac{x - 9}{9}$

13) $f(x) = 5$

14) $f(x) = 10$

15) $f(x) = 5x + 9$

16) $f(x) = x^2 + 3$

Find the inverse of the one-to-one function. Then, verify that $(f \circ f^{-1})(x) = x$, $(f^{-1} \circ f)(x) = x$, $D_f = R_{f^{-1}}$, and $R_f = D_{f^{-1}}$.

17) $f(x) = 4x + 3$

18) $f(x) = 5x + 5$

19) $f(x) = (x - 5)^3$

20) $f(x) = (x + 6)^3$

21) $g(x) = x^3 - 12$

22) $g(x) = x^3 - 9$

23) $f(x) = \sqrt{x + 2}$

24) $f(x) = \sqrt{x + 3}$

25) $h(x) = \frac{6 - x}{6}$

26) $h(x) = \frac{5 - x}{5}$

27) $g(x) = \frac{7}{x}$

28) $g(x) = \frac{6}{x}$

29) $f(x) = \sqrt[3]{x + 8}$

30) $f(x) = \sqrt[3]{x + 5}$

31) $g(x) = \frac{1 - x}{6x}$

32) $g(x) = x^3 + 4$

33) $f(x) = \sqrt{x + 9}$

34) $g(x) = \frac{11}{x}$

Determine if the functions are inverses of each other.

$$35) f(x) = 5x, g(x) = \frac{x}{5}$$

$$36) f(x) = 4x, g(x) = \frac{x}{4}$$

$$37) f(x) = x - 5, g(x) = x + 5$$

$$38) f(x) = x - 3, g(x) = x + 3$$

$$39) f(x) = 5x + 9, g(x) = \frac{x - 9}{5}$$

$$40) f(x) = 2x + 2, g(x) = \frac{x - 2}{2}$$

$$41) f(x) = 5x + 9, g(x) = 9 - 5x$$

$$42) f(x) = 6x + 4, g(x) = 4 - 6x$$

$$43) f(x) = x^3 + 2, g(x) = \sqrt[3]{x - 2}$$

$$44) f(x) = x^3 + 8, g(x) = \sqrt[3]{x - 8}$$

$$45) f(x) = x^5 + 3, g(x) = \sqrt[5]{x} - 3$$

$$46) f(x) = x^5 + 9, g(x) = \sqrt[5]{x} - 9$$

$$47) f(x) = 6x, g(x) = \frac{x}{6}$$

$$48) f(x) = 2x + 3, g(x) = \frac{x - 3}{2}$$

$$49) f(x) = 5x + 4, g(x) = 4 - 5x$$

$$50) f(x) = 5x + 6, g(x) = \frac{x - 6}{5}$$

$$51) f(x) = 8x, g(x) = \frac{x}{8}$$

$$52) f(x) = 7x + 4, g(x) = 4 - 7x$$

Solve the application.

53) When Miguel converted his Mexican pesos to U.S. dollars, the conversion function was represented by $f(x) = 13.4x$, where x represented the number of U.S. dollars. Find the inverse function f^{-1} and explain the meaning of the variables.

54) When Miguel converted his Mexican pesos to U.S. dollars, the conversion function was represented by $f(x) = 13.2x$, where x represented the number of U.S. dollars. Find the inverse function f^{-1} and explain the meaning of the variables.

55) When Pierre converted his Euros to British pounds, the conversion function was represented by $f(x) = 1.13x$, where x represented the number of British pounds. By finding the inverse function, determine how many British pounds Pierre received if he converted 1695 Euros. Round to the nearest pound, if necessary.

56) When Pierre converted his Euros to British pounds, the conversion function was represented by $f(x) = 1.13x$, where x represented the number of British pounds. By finding the inverse function, determine how many British pounds Pierre received if he converted 1808 Euros. Round to the nearest pound, if necessary.

57) Sandra earns a weekly salary of \$600 plus 4% on her total sales. If x represents the total dollar amount of her sales for one week, then $f(x) = 600 + 0.04x$ represents her weekly salary. Find the inverse function and explain the meaning of the variables.

58) Sandra earns a weekly salary of \$650 plus 7% on her total sales. If x represents the total dollar amount of her sales for one week, then $f(x) = 650 + 0.07x$ represents her weekly salary. Find the inverse function and explain the meaning of the variables.

59) Derek earns a weekly salary of \$600 plus 5% on his total sales. If x represents the total dollar amount of his sales for one week, then $f(x) = 600 + 0.05x$ represents his weekly salary. By finding the inverse function, determine Derek's total sales the week his salary was \$950.

60) Derek earns a weekly salary of \$500 plus 7% on his total sales. If x represents the total dollar amount of his sales for one week, then $f(x) = 500 + 0.07x$ represents his weekly salary. By finding the inverse function, determine Derek's total sales the week his salary was \$1130.

Answer Key

Testname: WORKSHEET 8.2B_GRAPHINGFUNCTIONWITHTHEINVERSE_V01

- 1) One-to-one, passes the horizontal line test
- 2) One-to-one, passes the horizontal line test
- 3) One-to-one, passes the horizontal line test
- 4) One-to-one, passes the horizontal line test
- 5) Not one-to-one, fails the horizontal line test
- 6) Not one-to-one, fails the horizontal line test
- 7) Not one-to-one, fails the horizontal line test
- 8) Not one-to-one, fails the horizontal line test
- 9) Not one-to-one, fails the horizontal line test
- 10) Not one-to-one, fails the horizontal line test
- 11) One-to-one, passes the horizontal line test
- 12) One-to-one, passes the horizontal line test
- 13) Not one-to-one, fails the horizontal line test
- 14) Not one-to-one, fails the horizontal line test
- 15) One-to-one, passes the horizontal line test
- 16) Not one-to-one, fails the horizontal line test
- 17) $f^{-1}(x) = \frac{x-3}{4}$
- 18) $f^{-1}(x) = \frac{x-5}{5}$
- 19) $f^{-1}(x) = \sqrt[3]{x} + 5$
- 20) $f^{-1}(x) = \sqrt[3]{x} - 6$
- 21) $g^{-1}(x) = \sqrt[3]{x+12}$
- 22) $g^{-1}(x) = \sqrt[3]{x+9}$
- 23) $f^{-1}(x) = x^2 - 2, x \geq 0$
- 24) $f^{-1}(x) = x^2 - 3, x \geq 0$
- 25) $h^{-1}(x) = -6x + 6$
- 26) $h^{-1}(x) = -5x + 5$
- 27) $g^{-1}(x) = \frac{7}{x}, x \neq 0$
- 28) $g^{-1}(x) = \frac{6}{x}, x \neq 0$
- 29) $f^{-1}(x) = x^3 - 8$
- 30) $f^{-1}(x) = x^3 - 5$
- 31) $g^{-1}(x) = \frac{1}{6x+1}, x \neq -\frac{1}{6}$
- 32) $g^{-1}(x) = \sqrt[3]{x-4}$
- 33) $f^{-1}(x) = x^2 - 9, x \geq 0$
- 34) $g^{-1}(x) = \frac{11}{x}, x \neq 0$
- 35) Yes
- 36) Yes
- 37) Yes
- 38) Yes

Answer Key

Testname: WORKSHEET 8.2B_GRAPHINGFUNCTIONWITHTHEINVERSE_V01

39) Yes

40) Yes

41) No

42) No

43) Yes

44) Yes

45) No

46) No

47) Yes

48) Yes

49) No

50) Yes

51) Yes

52) No

53) $f^{-1}(x) = \frac{x}{13.4}$; x represents the number of pesos, $f^{-1}(x)$ represents the number of U.S. dollars.

54) $f^{-1}(x) = \frac{x}{13.2}$; x represents the number of pesos, $f^{-1}(x)$ represents the number of U.S. dollars.

55) 1500 pounds

56) 1600 pounds

57) $f^{-1}(x) = \frac{x - 600}{0.04}$, where x represents her weekly salary and $f^{-1}(x)$ represents her total sales.

58) $f^{-1}(x) = \frac{x - 650}{0.07}$, where x represents her weekly salary and $f^{-1}(x)$ represents her total sales.

59) \$7000

60) \$9000